

Forecasting of Rice Production Using Fuzzy Time Series Representation through E-Commerce Website

Mohit Jain¹, Dr. Pankaj Dashore²

Computer Science and Engineering, Medicaps Institute of Technology & Management,
Indore (MP), India^{1,2}

mohit13_jain@yahoo.com¹, dashorepankaj@gmail.com²

Abstract: *Time-Series models are used for predictions in whether forecasting, academic enrollments, rice production etc. The concept of fuzzy time series is introduced by Song & Chissom in 1993. Over the past 24 years, many fuzzy time series methods have been proposed for rice production forecasting, but the forecasting accuracy rate of the existing methods is not good enough. These methods have used actual production, difference of production or percentage change in production as the universe of discourse. And frequency density based partitioning or ratio based partitioning for partition of discourse. This paper, proposed a method based on fuzzy time series, which gives the more accurate result than the existing methods. The proposed method used the actual production as the universe of discourse and mean based partitioning as partition of discourse. To illustrate the forecasting process, the historical data of rice production of University of Agriculture and Technology, India is used.*

Keywords: *fuzzy time series, mean square error, average forecast error rate.*

I. Introduction

Forecasting plays an important role every day. If there are uncertainties about the future, decision makers need to do forecast. Forecasting is the process for prediction of future outcomes. Decision makers examine the related data and graphs to take the best decisions for the future. The issues of time series forecasting has come into picture for mainly two reasons. First, most of the data existing in business, economic, and financial area are time series. Second, it is very easy to evaluate time series as many technologies are available for evaluation of time series forecast. Various techniques have been developed for time series forecasting in last few decade, but the classical time series technique can not deal with the forecasting issues in which the data of time series are represented by fuzzy sets [1]. To overcome this issue, the concept of fuzzy time series forecasting is given by Song & Chissom in 1993[2]. Fuzzy time series model deals with the both data foam numerical values and fuzzy sets.

Various fuzzy forecasting methods have been developed for different data sets for example enrollment forecasting ([1] - [15]), car fatalities ([16] - [17]), food grain production [18], population forecasting [19] and rice production forecasting [20]. These methods used different values for universe of discourse for example the methods proposed in [3] and [8] used the differences of the enrollments and the method in [10] used the percentage change. And for partition of discourse these models used frequency density petitioning or ratio based partitioning. These fuzzy time series models have also been used to solve different domain problems for example whether forecasting, financial forecasting etc.

The main objective of this paper is to make and implement the fuzzy time series method for rice production forecasting with higher forecast accuracy rate, and comparison of the result with existing forecasting methods.

The basic definitions of fuzzy time series are described in section 2. The new method has developed in section 3 which used the historical data of rice production of University of Agriculture and Technology, India.

Comparison of the result of proposed method with the result of the existing method has done in section 4. Finally the concluding remarks are discussed in section 5.

II. CONCEPT OF FUZZY TIME SERIES

Definition 1: Fuzzy Set

Fuzzy sets are sets whose elements contain degree of membership.

Let U be the universe of discourse, $U = \{u_1, u_2, \dots, u_n\}$, and let A be a fuzzy set in the universe of discourse U defined as follows:

$$A = f_A(u_1) / u_1 + f_A(u_2) / u_2 + \dots + f_A(u_n) / u_n,$$

Where f_A is the membership function of A , $f_A: U \rightarrow [0, 1]$, $f_A(u_i)$ indicates the grade of membership of u_i in the fuzzy set A , $f_A(u_i) \in [0, 1]$, and $1 \leq i \leq n$, [1].

Definition 2: Time Series

A time series is a collection of sequential data points, measured at successive time span at uniform time intervals.

Definition 3: Fuzzy Time Series

Consecutive sequences of indefinite data are considered as time series with fuzzy data. A time series with fuzzy data is referred to as fuzzy time series. [9]. Let $X(t)$ ($t = \dots, 0, 1, 2, \dots$) be the universe of discourse and be a subset of R , and let fuzzy set $f_i(t)$ ($i = 1, 2, \dots$) be defined in $X(t)$. Let $F(t)$ be a collection of $f_i(t)$ ($i = 1, 2, \dots$). Then, $F(t)$ is called a fuzzy time series of $X(t)$ ($t = \dots, 0, 1, 2, \dots$) [1].

Definition 4: Time variant and Time-invariant fuzzy time series

Let $F(t)$ be a fuzzy time series and let $R(t, t - 1)$ be a first-order model of $F(t)$. If $R(t, t - 1) = R(t - 1, t - 2)$ for any time t , then $F(t)$ is called a time-invariant fuzzy time series.

If $R(t, t - 1)$ is dependent on time t , that is, $R(t, t-1)$ may

be different from $R(t - 1, t - 2)$ for any t , then $F(t)$ is called a time-variant fuzzy time series, [1].

Definition 5: First order model

If $F(t)$ is caused by $F(t - 1)$, denoted by $F(t - 1) \rightarrow F(t)$, then this relationship can be represented by $F(t) = F(t - 1) \circ R(t, t - 1)$, where the symbol " \circ " denotes the Max-Min composition operator; $R(t, t - 1)$ is a fuzzy relation between $F(t)$ and $F(t - 1)$ and is called the first-order model of $F(t)$, [1].

Definition 6: Forecast Error

A forecast error is defined as the difference between the actual value and the forecast value of a time series.

$$\text{Error} = \text{Actual value} - \text{forecasted value.}$$

III. PROPOSED METHOD

This section, proposed a new method for rice production forecasting by using actual production as the universe of discourse and mean based partitioning. The historical data of rice production of University of Agriculture and Technology, India are shown in Table I [20].

The forecasting process follows the following steps:

Step 1: Firstly, define the universe of discourse U and Partition U into equally length intervals.

Step 2: Define fuzzy sets X_i , and apply fuzzification.

Step 3: Apply Forecast and defuzzification on the forecasted output.

TABLE I.
THE HISTORICAL DATA OF RICE PRODUCTION [20]

Year	Production (Kg/hect.)
81-82	2730
82-83	2957
83-84	2382
84-85	2572
85-86	2642

86-87	2700
87-88	2872
88-89	3407
89-90	2238
90-91	2895
91-92	3276
92-93	1431
93-94	2248
94-95	2857
95-96	2318
96-97	2617
97-98	2254
98-99	2910
99-00	3434
00-01	2795
01-02	3000

Step 1: Take the historical data of rice production as shown in Table I and define the universe of discourse U for example, assume $U=[1400, 3500]$ and partition it into intervals of equal length. Assume 7 equal intervals shown in Table II. Now find the frequency of each interval.

MEANS OF ORIGINAL DATA AND FREQUENCY OF INTERVALS DATA

Interval	Number of Data
[1400, 1700]	1
[1700-2000]	0
[2000-2300]	3
[2300-2600]	3
[2600-2900]	8
[2900-3200]	3
[3200-3500]	3

Step 2: Split all seven intervals into sub-intervals using mean based partitioning. Define fuzzy set X_i for each sub-interval shown in Table III.

TABLE II.
FUZZY INTERVALS USING MEAN BASED PARTITIONING

Linguistic Variable	Interval
X_1	[1400, 1700]
X_2	[2000, 2100]
X_3	[2100, 2200]
X_4	[2200, 2300]
X_5	[2300, 2400]
X_6	[2400, 2500]
X_7	[2500, 2600]
X_8	[2600, 2637.5]
X_9	[2637.5, 2675]
X_{10}	[2675, 2712.5]
X_{11}	[2712.5, 2750]
X_{12}	[2750, 2787.5]
X_{13}	[2787.5, 2825]
X_{14}	[2825, 2862.5]
X_{15}	[2862.5, 2900]
X_{16}	[2900, 3000]
X_{17}	[3000, 3100]
X_{18}	[3100, 3200]
X_{19}	[3200, 3300]
X_{20}	[3300, 3400]
X_{21}	[3400, 3500]

Step 3: Apply defuzzification using the Centroid method on the fuzzy sets which are generated in step 2. The defuzzification is shown in Table IV.

IV. A COMPARISON OF DIFFERENT FORECASTING METHODS

This paper used two parameters to compare result of proposed method with the existing method. First, average forecasting error rate (AFER) and second, mean square error (MSE). The comparison of different forecasting methods shown in Table V:

$$AFER = (|A_i - F_i| / A_i) / n \times 100\%$$

$$MSE = (\sum_{i=1}^n (A_i - F_i)^2) / n$$

Where A_i denotes the actual population and F_i denotes the forecasting population of year i , respectively. In [20] fuzzy time series method

AFER and MSE comes to 20.83% and 384987.6, respectively, where as for proposed fuzzy time series method has 2.29% and 19198.2381, respectively. Fig1 shows the comparison of different forecasting methods.

TABLE III.
FORECASTING RESULT OF THE PROPOSED METHOD

Year	Production (A_i)	Fuzzy set	Forecast (F_i)	$A_i - F_i$	$(A_i - F_i)^2$	$ A_i - F_i / A_i$
1991	2730	X_{11}	2450	280	78400	0.1025
1992	2957	X_{16}	2950	7	49	0.0023
1993	2382	X_5	2350	32	1024	0.0134
1994	2572	X_7	2550	22	484	0.0085
1995	2642	X_3	2650	-8	64	0.0030
1996	2700	X_{10}	2690	10	100	0.0037
1997	2872	X_{15}	2880	-8	64	0.0027
1998	3407	X_{21}	3450	-43	1849	0.0126
1999	2238	X_4	2250	-12	144	0.0053
2000	2895	X_{15}	2880	15	225	0.0051
2001	3276	X_{19}	3250	26	676	0.0079
2002	1431	X_1	1550	-119	14161	0.0831
2003	2248	X_4	2250	-2	4	0.0008
2004	2857	X_{14}	2840	17	289	0.0059
2005	2318	X_5	2350	-32	1024	0.0138
2006	2617	X_8	2620	-3	9	0.0011
2007	2254	X_4	2250	4	16	0.0017
2008	2910	X_{16}	2950	-40	1600	0.0137
2009	3434	X_{21}	3450	-16	256	0.0046
2010	2795	X_{13}	2810	-15	225	0.0053
2011	3000	X_{16}	2450	550	302500	0.1833
					MSE = 19198.2381	AFER = 2.2871%

TABLE IV.
COMPARISON OF DIFFERENT FORECASTING METHODS

Year	Production	Forecasted Production [32]	Proposed Method
1991	2730	-	2450
1992	2957	2723	2950
1993	2382	3011	2350
1994	2572	2411	2550
1995	2642	2489	2650
1996	2700	2711	2690
1997	2872	2723	2880
1998	3407	2789	3450
1999	2238	3250	2250
2000	2895	2189	2880
2001	3276	2789	3250
2002	1431	3217	1550
2003	2248	1650	2250
2004	2857	2189	2840
2005	2318	2789	2350
2006	2617	2411	2620
2007	2254	2711	2250
2008	2910	2146	2950
2009	3434	3089	3450
2010	2795	3250	2810
2011	3000	2789	2450
AFER	-	20.83%	2.29%
MSE	-	384987.6	19198.2381

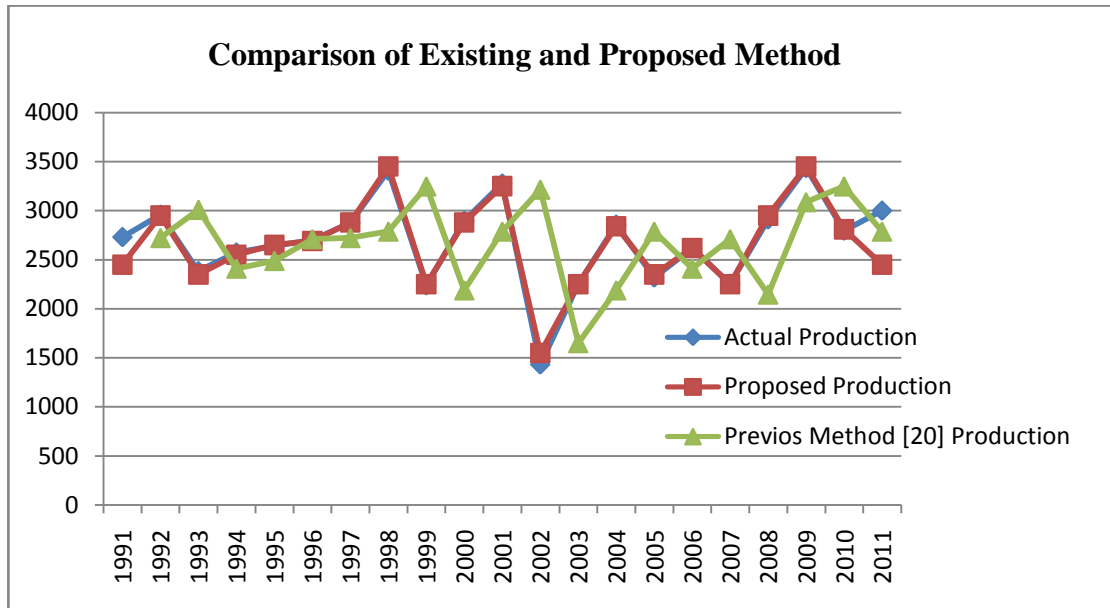


Fig1: Comparison of different forecasting methods



Fig2 : Representation through E-Commerce Website

V. CONCLUSION

This paper, proposed a new method with higher forecast accuracy rate. From Table V, it is clear that as the error rate decreases, accuracy rate increases. Future work includes the development of new method for different domain with different intervals to get a higher forecasting accuracy.

References

- [1] S. M. Chen and Hsu, "A new method to forecasting enrollments using fuzzy time series", *International Journal of Applied Science and Engineering*, vol. 2, no. 3, pp. 234-244, 2004.
- [2] Q. Song and B. S. Chissom, "Forecasting enrollments with fuzzy time series: Part II", *Fuzzy Sets and systems*, vol. 62: pp. 1-8, 1994.
- [3] S. M. Chen, "Forecasting enrollments based on fuzzy time series", *Fuzzy Sets and Systems*, vol. 81, pp. 311-319, 1996.
- [4] J. R. Hwang, S. M. Chen and C. H. Lee, "Handling forecasting problems using fuzzy time series", *Fuzzy Sets and Systems*, vol. 100, pp. 217-228, 1998.
- [5] K. Huarng, "Effective length of intervals to improve forecasting in fuzzy time series", *Fuzzy Sets and systems*, vol. 12, pp. 387-394, 2001.
- [6] S. M. Chen, "Forecasting enrollments based on high-order fuzzy time series", *Cybernetics and Systems: An International Journal*, vol. 33, pp. 1-16, 2002.
- [7] S. Melike and K.Y. Degtiarev, "Forecasting enrollments model based on first- order fuzzy time series", *Proceedings of World Academy of Science, Engineering and Technology*, vol. 1, pp. 132-135, 2005.
- [8] T. A. Jilani, S. M. A. Burney and C. Ardil, "Fuzzy metric approach for fuzzy time series forecasting based on frequency density based partitioning", *Proceedings of World Academy of Science, Engineering and Technology*, vol. 34, pp. 333-338, 2007.
- [9] Stevenson and Porter, "Fuzzy time series forecasting using percentage change as the universe of discourse", *Proceedings of World Academy of Science, Engineering and Technology*, vol. 55, pp. 154-157, 2009.
- [10] Z. Ismail and R. Efendi, "Enrollment forecasting based on modified weight fuzzy time series", *Journal of Artificial Intelligence*, vol. 4, no.1, pp. 110-118, 2011.
- [11] Arutehelvan G., Sivatsa S. K and Jaganathan R., "Inaccuracy minimization by partitioning fuzzy data sets- validation of an analytical methodology", *International Journal of Computer Science and Information Security*, vol. 8, no. 1, 2010.
- [12] Q. Song and B. S. Chissom, "Fuzzy time series and its models", *Fuzzy Sets and systems*, vol. 54, pp. 269-277, 1993.
- [13] Q. Song and B. S. Chissom, "Forecasting enrollments with fuzzy time series: Part I", *Fuzzy Sets and systems*, vol. 54, pp. 1-9, 1993.
- [14] Liang Zhao, "A new method to predict enrollments based on fuzzy time series", *proceeding of the 8th World Congress on Intelligent Control and Automation (IEEE)*, pp. 3201-3206, 2010.
- [15] W. K. Wong, E. Bai and A. W. Ching Chu, "Adaptive time-variant models for fuzzy time series forecasting", *IEEE Transactions on Systems, Man, And Cybernetics- Part B: Cybernetics*, vol. 40, no. 6, pp. 1531- 1542, 2010.